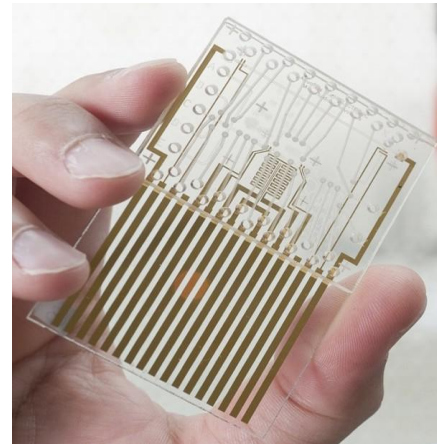
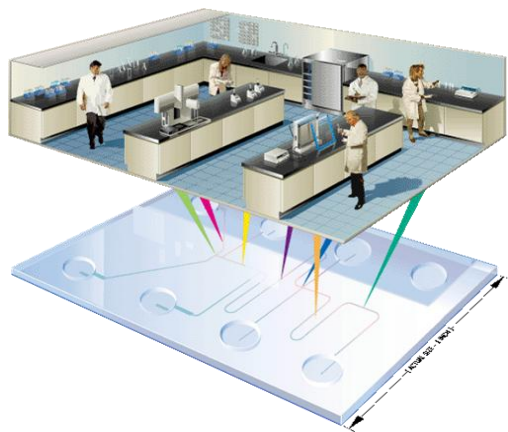




Converging Artificial Intelligence (AI) and Capillary Microfluidics simulation in Lab-on-a-chip



Academic Supervisor: Dr. A. Tarokh, Lakehead University

Partner organization: Dr. M. Saboori, Hudson International Consultant and Investment

Intern: Dr. A. Amiri Delouei, Lakehead University



Dear Dr. Saboori,

I would like to inform you that I have successfully completed **Stage 1 (literature review)** and **Stage 2 (CFD analysis)** of the project outlined in the Mitacs proposal and will now continue with the next stage.

In the next slides, I will also present results from studies that are published or ready to be published, including the following titles:

- *A Comprehensive Analysis of Capillary Penetration in Circular and Rectangular Microchannels*
- *Capillary Transport Behavior in Elliptical Microchannels Based on Theoretical Modeling*
- *Direct Numerical Simulation of Capillary Microfluids: Lattice Boltzmann Method*

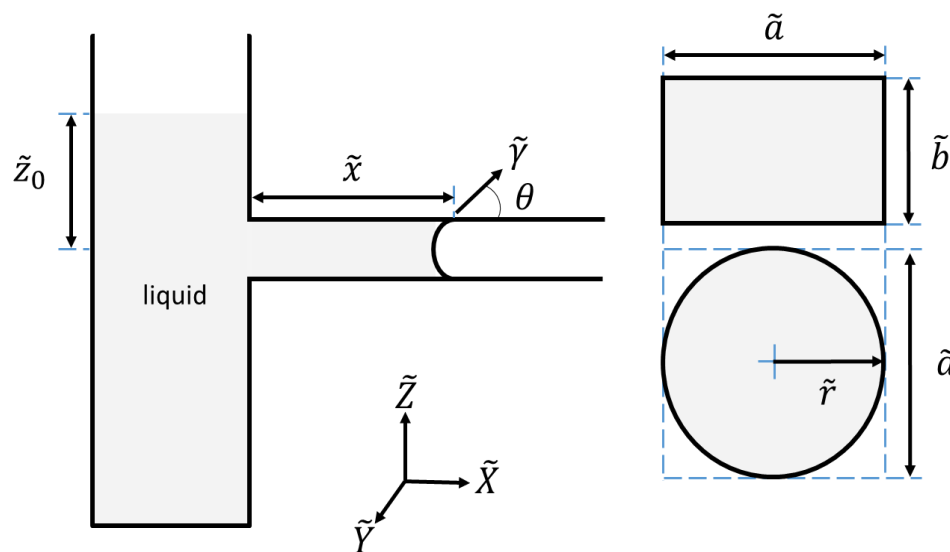


A Comprehensive Analysis of Capillary Penetration in Circular and Rectangular Microchannels

3

Introduction:

This research presents an analytical examination of the **capillary penetration phenomenon**. In this research, a laminar and incompressible flow in circular and rectangular ducts is considered.

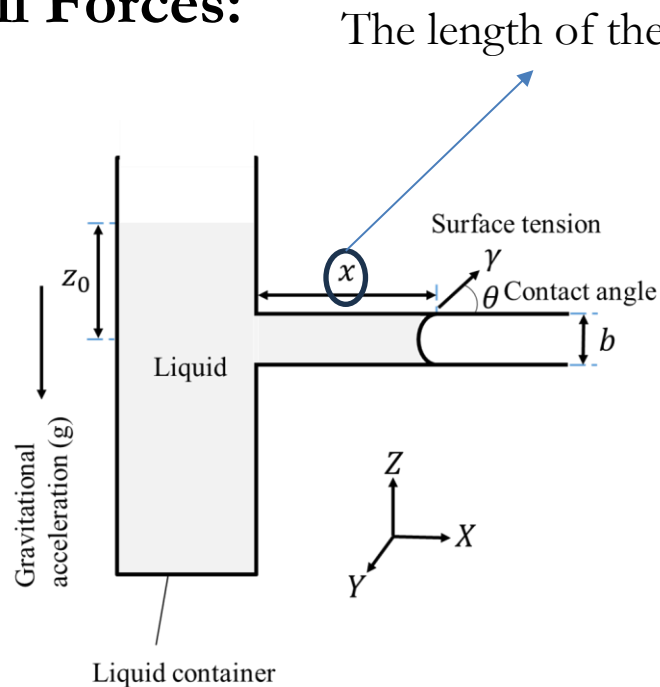




A Comprehensive Analysis of Capillary Penetration in Circular and Rectangular Microchannels

4

All Forces:



All Forces

the momentum of the liquid column

F_m

hydrostatic pressure

F_h

capillary

F_c

viscous (retarding)

F_v

The Motion equation:

Capillary Penetration in Microchannels.

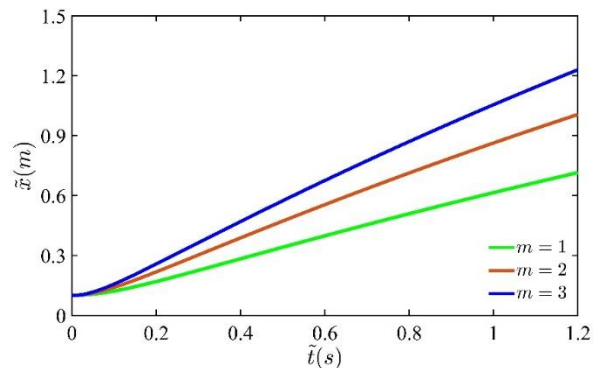
$$\frac{dF_m}{dt} = F_h + F_c - F_v$$



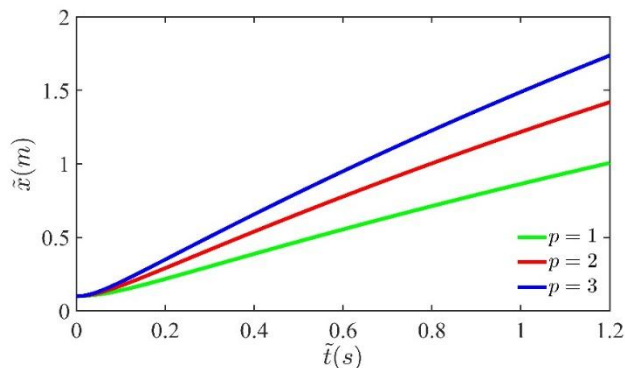
A Comprehensive Analysis of Capillary Penetration in Circular and Rectangular Microchannels

5

Results:



Variation of the column length versus time for different values of m in circular ($n = 1$) cross-sections at $\tilde{x}_0 = 0.1(m)$



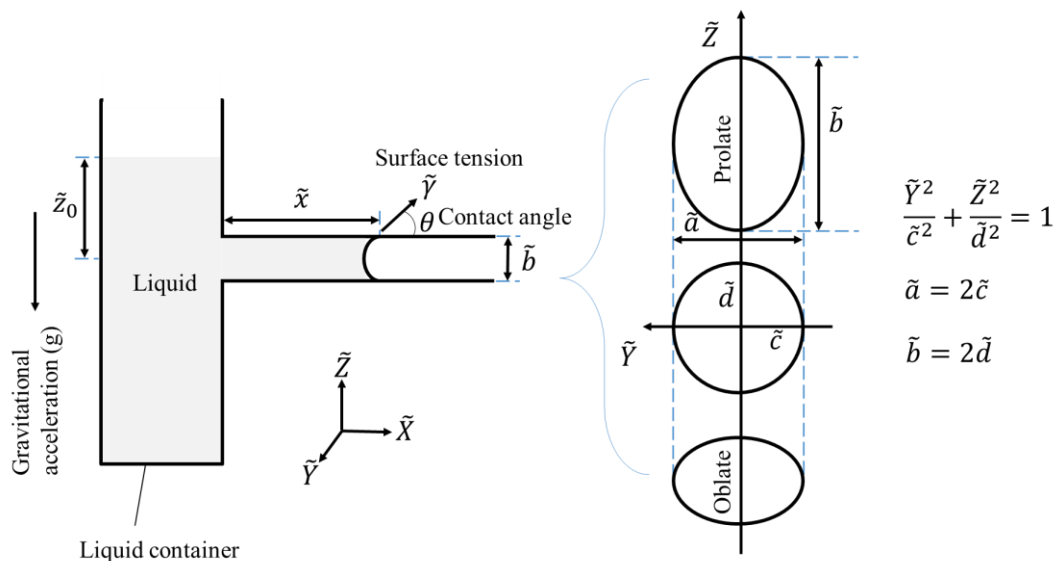
Variation of the column length versus time for different values of p in rectangular ($q = 1$) cross-sections at $\tilde{x}_0 = 0.1(m)$



Capillary Transport Behavior in Elliptical Microchannels Based on Theoretical Modeling

6

Introduction: This research presents a comprehensive theoretical investigation into the capillary penetration phenomenon within **elliptical microchannels**. This study develops a detailed mathematical framework for analyzing the process by focusing on the governing equations, initial conditions, and solution methods within a two-dimensional context.



Capillary Transport Behavior in Elliptical Microchannels Based on Theoretical Modeling



7

Analytical solution:

After considering all the forces, the equation can be analytically solved by considering the initial conditions.

$$x^2 - x_0^2 = \underbrace{\alpha}_{\text{Capillary force}} (\beta t + \exp(-\beta t) - 1) \underbrace{\beta}_{\text{Viscous force}}$$

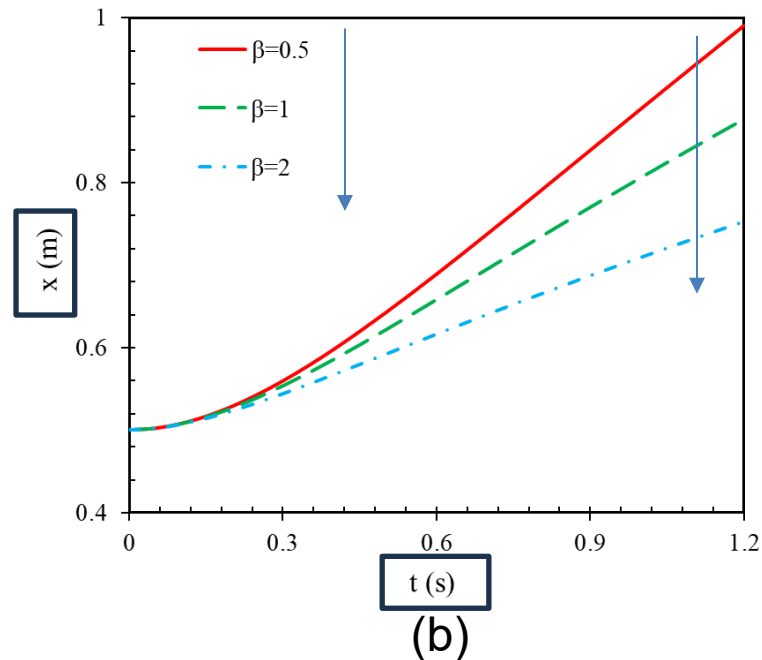
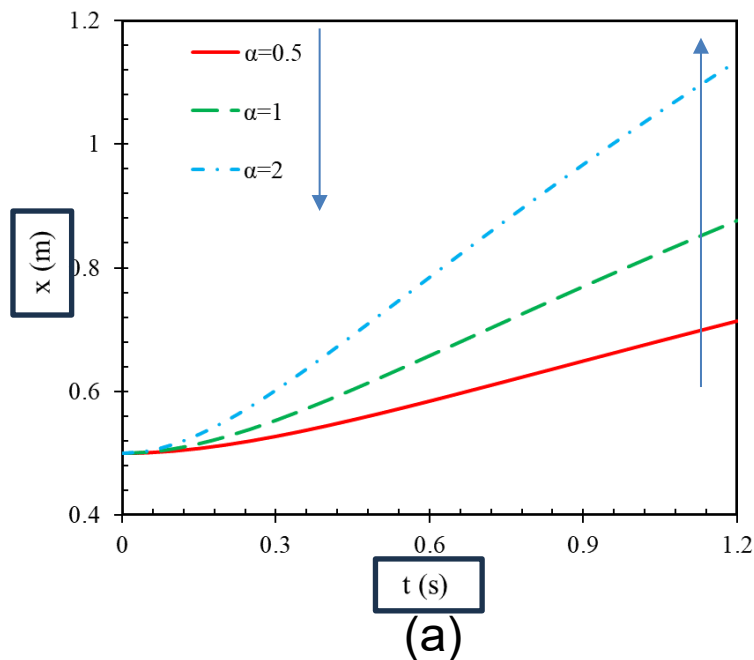
$$\frac{16\gamma \cos \theta \sqrt{a^2 + b^2}}{\sqrt{8}\delta ab} + 2gz_0 \qquad \frac{16\mu(a^2 + b^2)}{\delta a^2 b^2}$$



Capillary Transport Behavior in Elliptical Microchannels Based on Theoretical Modeling

8

The effect of capillary and viscous forces on x :



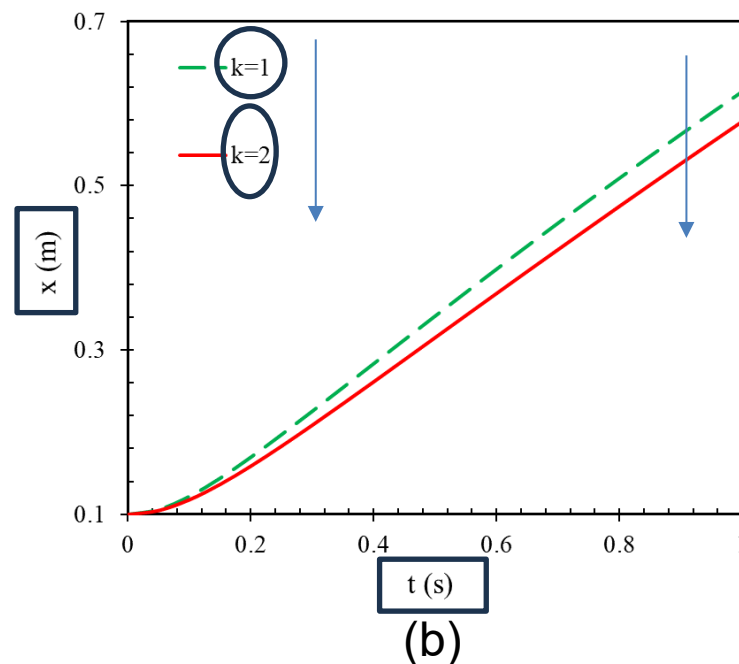
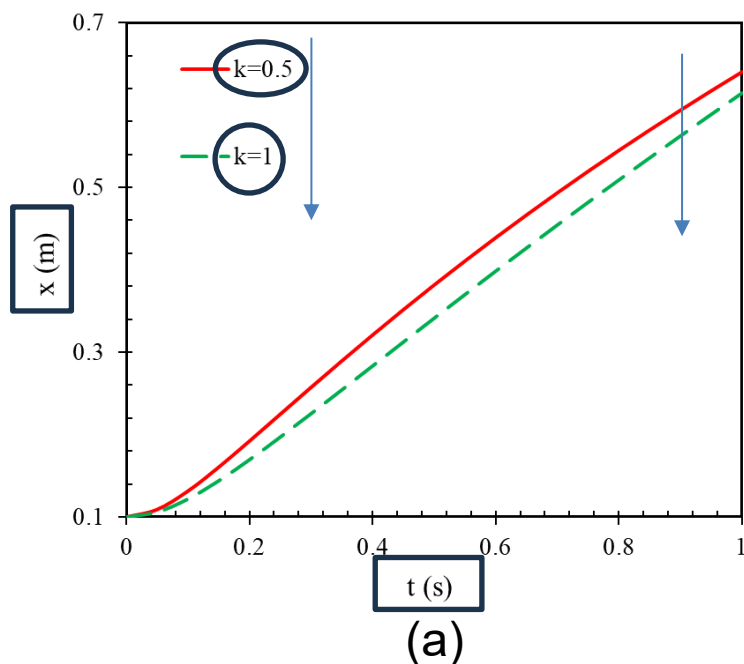
Variation of x versus time for different value of (a) α , and (b) β .



Capillary Transport Behavior in Elliptical Microchannels Based on Theoretical Modeling

9

The effect of aspect ratio ($k = b/a$) on x :



Variation of x versus time for different shape at $x_0 = 0.1$ (a) oblate and circular shapes, and (b) circular and prolate shapes.

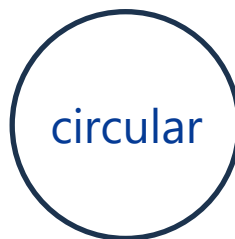
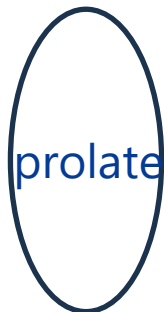


Capillary Transport Behavior in Elliptical Microchannels Based on Theoretical Modeling

10

All Findings:

- An increase in the value of α indicates an increase in the capillary force. Consequently, the length of the column increases in response to the surface tension.
- The parameter β in the study exhibits as an indicator of the viscous force, and its augmentation results in a reduction of the penetration flow.
- Enhancing the penetration flow with decreasing the aspect ratio in the same cross-section



Enhancing the penetration flow in the same cross-section

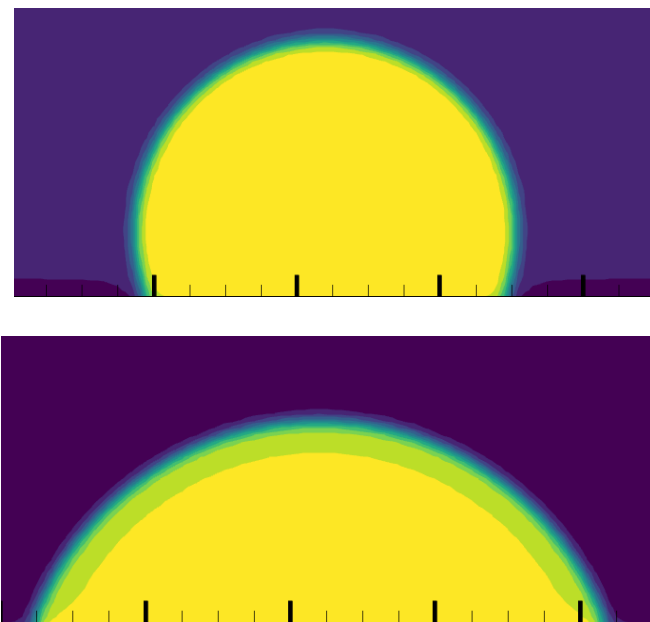




Direct Numerical Simulation of Capillary Microfluids: Lattice Boltzmann Method

11

Introduction: This research employs the lattice Boltzmann method (LBM) to model the motion of a two-phase flow in a microchannel. The fluid flow in this system is primarily driven by surface tension. To validate the accuracy of the developed code, simulations of a droplet on both hydrophilic and hydrophobic surfaces are conducted, yielding successful results. These findings demonstrate the strong capability of the LBM in accurately simulating surface-tension driven flows in microfluidic systems.



Droplet on hydrophilic and hydrophobic surfaces

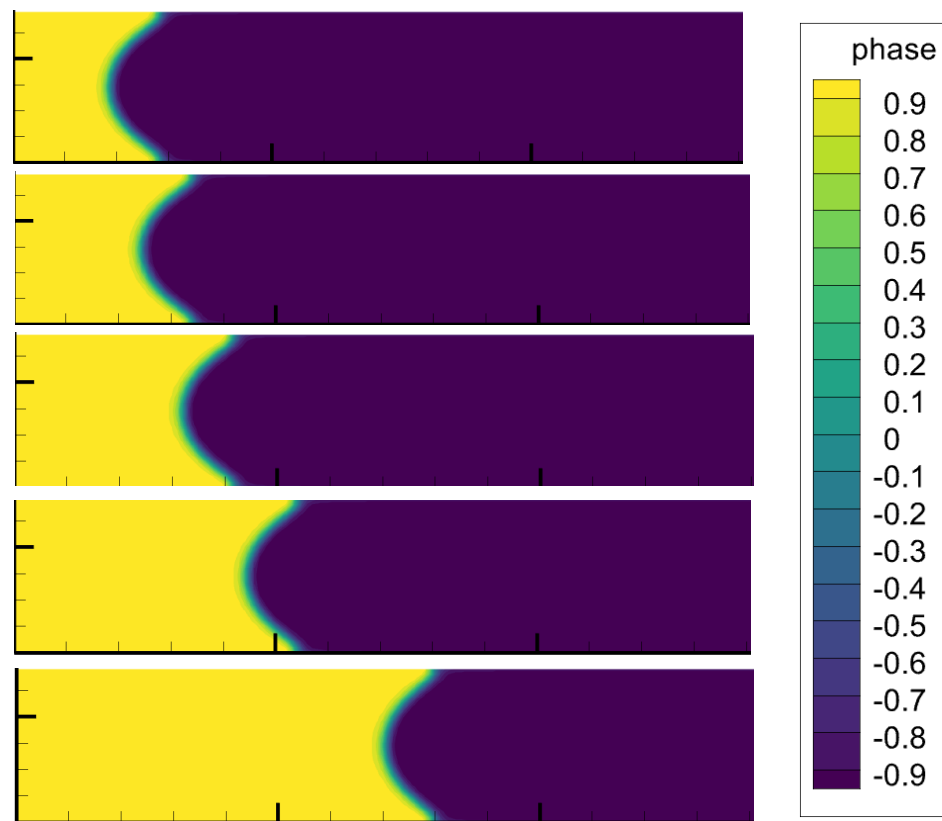


Direct Numerical Simulation of Capillary Microfluids: Lattice Boltzmann Method

12

Results for two-phase flow interface
in a microchannel:

The simulation results demonstrate the effectiveness of the lattice Boltzmann method (LBM) as an efficient approach for conducting Direct Numerical Simulation (DNS) of Capillary Microfluids.



Interface surface in different positions